

**SOME FIXED POINT THEOREMS WITH RATIONAL TYPE  
CONTRACTION IN CONTROLLED METRIC SPACES**

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**ABSTRACT.** In this paper, we extend some fixed point theorems with rational type contraction from metric spaces to controlled metric spaces. The results are the generalizations of [10, 12, 13]. Moreover, we give some examples to confirm our results.

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*Received:* July 27, 2022. *Revised:* November 15, 2022.

*2010 Mathematics Subject Classification:* 47H10, 54H25.

*Key words and phrases:* Fixed point, controlled metric space, rational type contraction.

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