

## THE TOTIENT PROBLEM

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ABSTRACT. A solution to the totient problem is given. It depends on two identities for the function  $\varphi(n)$ . A connection with prime pairs differing by 2 is described.

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