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REPRESENTATIONS OF WEIGHTED ROTA-BAXTER JACOBI-JORDAN ALGEBRAS

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Abstract. Weighted Rota-Baxter Jacobi-Jordan algebras and their representations are studied. Moreover, we consider weighted Rota-Baxter paired operators that are related to weighted Rota-Baxter Jacobi-Jordan algebras together with their representations. Finally, we define suitable cohomology for weighted Rota-Baxter Jacobi-Jordan algebras in low degrees.

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