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VALUE DISTRIBUTION OF GENERAL q-DIFFERENCE-DIFFERENTIAL POLYNOMIALS OF A MEROMORPHIC FUNCTION

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Abstract. The main purpose of this paper is to investigate the growth condition as well as the distribution of zeros of the most general polynomial generated by shifts, q-shifts and derivatives of a meromorphic function. Meanwhile the results obtained in this paper not only generalize but also improve the earlier results of Zheng and Xu [20] by removing the conditions on the zeros and poles of a meromorphic function.

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