J. Adv. Math. Stud.
Vol. **15**(2022), No. 3, 274-287
http://journal.fairpartners.ro

SOME RESULTS ON NONLINEAR MIXED FRACTIONAL INTEGRODIFFERENTIAL EQUATIONS

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Abstract. In this paper, we study the existence, uniqueness and other properties of solutions for the special class of fractional Volterra Fredholm integrodifferential equation involving Caputo fractional derivative $n-1 < \alpha \leq n$, $n > 1$. The result of existence and uniqueness is obtained with help of well known Banach contraction principle and the integral inequality which provides explicit bound on the unknown function. The obtained some results are illustrated through example.

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Received: January 17, 2022. *Revised:* May 29, 2022.
2010 *Mathematics Subject Classification*: 26A33, 34A08, 34A12, 47H10.
Key words and phrases: Fractional mixed integrodifferential equation, existence and uniqueness of solution, fixed point theorem, integral inequality.

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