

b -METRIC SPACE, DISLOCATED b -METRIC SPACE AND GERAGHTY TYPE CONTRACTIONS

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ABSTRACT. In this paper, we obtain common fixed point results in b -metric space as well as in dislocated b -metric space for Geraghty type and ψ -Geraghty type contractions. These results extend some existing results in the literature. Moreover, some examples and an application for non-linear integral equations are also given.

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